

## SUBJECT TEACHING GUIDE

### G84 - Further Differential Calculus

#### Double Degree in Physics and Mathematics Degree in Mathematics

Academic year 2021-2022

| 1. IDENTIFYING DATA              |   |                  |                    |                  |  |
|----------------------------------|---|------------------|--------------------|------------------|--|
| Degree                           | Double Degree in Physics and Mathematics<br>Degree in Mathematics                             |                  |                    | Type and Year    | Compulsory. Year 2<br>Compulsory. Year 2 |
| Faculty                          | Faculty of Sciences   |                  |                    |                  |  |
| Discipline                       | Subject Area: Mathematical Analysis and Differential Equations<br>Module: Compulsory Subjects |                  |                    |                  |  |
| Course unit title and code       | G84 - Further Differential Calculus   |                  |                    |                  |  |
| Number of ECTS credits allocated | 6   | Term             | Semester based (1) |                  |  |
| Web                              | <a href="https://personales.unican.es/stand/">https://personales.unican.es/stand/</a>         |                  |                    |                  |  |
| Language of instruction          | Spanish   | English Friendly | Yes                | Mode of delivery | Face-to-face                             |

|                  |   |  |  |  |  |
|------------------|---|--|--|--|--|
| Department       | DPTO. MATEMATICAS, ESTADISTICA Y COMPUTACION                              |  |  |  |  |
| Name of lecturer | CARLOS BELTRAN ALVAREZ  |  |  |  |  |
| E-mail           | carlos.beltran@unican.es  |  |  |  |  |
| Office           | Facultad de Ciencias. Planta: + 1. DESPACHO CARLOS BELTRAN ALVAREZ (1040) |  |  |  |  |
| Other lecturers  | JESUS ARAUJO GOMEZ  |  |  |  |  |

### 3.1 LEARNING OUTCOMES

- To understand the meaning of the properties of limit and continuity of functions of one and several variables . To know the proofs and apply the theorems to solve problems about continuity and uniform continuity of functions of one and several variables. Build proofs of some simple results on continuity.
- To understand the properties of differentiability of functions using geometric interpretation of the derivative and directional derivatives. Knowing the proofs and apply the theorems to solve problems of differentiability of functions of one and several variables. Build proofs of some simple results on differentiability.
- To know the fundamental theorems of differential calculus and its application to approach and solve basic problems of inverse and implicit functions, and approximation of functions by power series.

#### 4. OBJECTIVES

To understand the mathematical method in the theoretical development: definitions and axioms, propositions and theorems, examples and counter-examples.

To know different mathematical methods to get proofs of results and to be able to apply them for building proofs of simple results. Distinguish between right and wrong reasoning in simple proofs.

To acquire certain ability in handling the mathematical language for the formal statement of properties of sets and functions, as an initiation into the capacity to communicate in the context of this branch of science to an expert audience.

To acquire some skill in handling and interpretation of sets and functions using their properties and graphical interpretation.

To know some fundamental theorems of differential calculus, and their proofs.

The subject therefore complements the course of Differential Calculus, taught in the first year, which gives special attention to the most technical aspect of the issue.

#### 6. COURSE ORGANIZATION

##### CONTENTS

|   |   |
|---|---|
| 1 | Fundamental properties of $\mathbb{R}$ and $\mathbb{R}^n$   |
| 2 | Limits and continuity of functions  |
| 3 | Differentiable functions: derivatives of 1 variable functions, directional derivatives, partial derivatives, differentiable functions and chain rule. |
| 4 | Some important theorems   |
| 5 | Applications: Inverse function and implicit function theorems   |
| 6 | Applications 2: Taylor theorem, power series and function approximation.  |
| 7 | Uniform continuity of functions   |
| 8 | Evaluation  |

#### 7. ASSESSMENT METHODS AND CRITERIA

| Description   | Type         | Final Eval. | Reassessn | %      |
|---|--------------|-------------|-----------|--------|
| Partial exam during the course (40%)  | Written exam | No          | Yes       | 40,00  |
| Final exam (60%)  | Written exam | Yes         | Yes       | 60,00  |
| TOTAL   |              |             |           | 100,00 |
| Observations  |              |             |           |        |
| Observations for part-time students   |              |             |           |        |
| Part-time students may chose between getting their grade as the other students or being evaluated only by the final exam. |              |             |           |        |

#### 8. BIBLIOGRAPHY AND TEACHING MATERIALS

##### BASIC

J.E. Marsden y M.J. Hoffman. "Análisis Clásico Elemental". Ed. Addison-Wesley Iberoamericana

T. E. Apostol, "Calculus Volume II - Multivariable Calculus and Linear Algebra, with Applications to Differential Equations and Probability", Wiley, 2nd ed, 1969.

