# SUBJECT TEACHING GUIDE 

G2003 - Probability
Double Degree in Physics and Mathematics Degree in Mathematics

Academic year 2023-2024


| Department | DPTO. MATEMATICAS, ESTADISTICA Y COMPUTACION |
| :--- | :--- |
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| Other lecturers | JUAN ANTONIO CUESTA ALBERTOS <br> ALICIA NIETO REYES |

### 3.1 LEARNING OUTCOMES

- Knowledge and use of the basic concepts of probability.
- It aims an advanced manipulation of the fundamental tools of probability


## 4. OBJECTIVES

It is intended to give a correct formalization of the basic concepts of probability and study sequences of independent random variables and associated limit theorems.

| 6. COURSE ORGANIZATION |  |
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| CONTENTS |  |
| 1 | PROBABILITY SPACES. General probability spaces. Probability measures on the real line. |
| 2 | RANDOM VARIABLES. Random variable. Distribution functions of random variables. |
| 3 | RANDOM VECTORS. INDEPENDENCE. Random Vectors. Marginal probability. Conditional probability. Independence. |
| 4 | MEAN AND MOMENTS OF HIGHER ORDER. Expected value of a random variable. Moments of higher order. <br> Inequalities |
| 5 | SEQUENCES OF RANDOM VARIABLES. CONVERGENCE. Almost sure convergence, convergence in probability <br> and convergence in law. |
| 6 | LIMIT THEOREMS. An introduction to the Law of Large Numbers, Borel-Cantelli Theorems and Central Limit <br> Theorem. |
| 7 | Final exam |
| 8 | Tutorial |


| 7. ASSESSMENT METHODS AND CRITERIA | Type | Final Eval. | Reassessn | $\%$ |
| :--- | :--- | :--- | :--- | :--- |
| Description | Others | No | Yes | 40,00 |
| Continuous evaluation | Written exam | Yes | Yes | 60,00 |
| Final evaluation |  | 100,00 |  |  |
| TOTAL |  |  |  |  |
| Observations |  |  |  |  |
| Taking part in any of the activities of evaluation implies that the student has undergone the evaluation process. |  |  |  |  |
| Observations for part-time students |  |  |  |  |
| The assessment of part-time students follow the same rules as the assessment of full-time students. Taking part in any of the <br> two activities of evaluation implies that the student has done the evaluation |  |  |  |  |

## 8. BIBLIOGRAPHY AND TEACHING MATERIALS

## BASIC

CUESTA ALBERTOS (2006). Apuntes de Cálculo de Probabilidades
VELEZ IBARROLA, R. (2004) Cálculo de Probabilidades 2. Ediciones Académicas. Madrid
WILLIAMS, D. (2001). Weighing the odds: A course in probability and statistics. Cambridge University Press. Cambridge

