# SUBJECT TEACHING GUIDE 

## G36 - Mathematics II: Differential Calculus

## Degree in Physics <br> Degree in Physics

Academic year 2023-2024

| 1. IDENTIFYING DATA |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Degree | Degree in Physics Degree in Physics |  |  | Type and Year | Core. Year 1 Core. Year 1 |
| Faculty | Faculty of Sciences |  |  |  |  |
| Discipline | Subject Area: Basic Mathematics for Science Basic Module |  |  |  |  |
| Course unit title and code | G36-Mathematics II: Differential Calculus |  |  |  |  |
| Number of ECTS crenits allnc.ated | 6 | Term |  | Semester based (1) |  |
| Web |  |  |  |  |  |
| Language of instruction | Spanish | English Friendly | Yes | Mode of delivery | Face-to-face |


| Department | DPTO. MATEMATICAS, ESTADISTICA Y COMPUTACION |
| :--- | :--- |
| Name of lecturer | BEATRIZ PORRAS POMARES |
| E-mail | beatriz.porras@unican.es |
| Office | Facultad de Ciencias. Planta: + 3. DESPACHO (3019) |
| Other lecturers |  |

### 3.1 LEARNING OUTCOMES

- The knowledge about concepts and methods of matematical languaje as a tool for modelitation.
- Use of matrix, points, vectors, functions, polynomials, sequences, series, diferential equations and integrals.
-Knowing a relevant set of samples and situations that serve to improve intuition about concepts such as plane, movement,
limit, derivative or integral, both in one and several variables.
- Improve the skills for mathematical modelitation and computation of simple phisical problems


## 4. OBJECTIVES

To know, understand and handle a number of basic concepts and results concerning functions of one real variable:

- Equations and inequations with absolute values.
- Sequences and series in R; study of their convergence.
- Taylor series

To know, understand and apply basic results about functions of several real variables: limits, continuity, partial derivatives and differentials..., and apply them in problems of implicit functions, maxima and minima.

## 6. COURSE ORGANIZATION

## CONTENTS

1 REAL NUMBERS: SEQUENCES AND SERIES OF REAL NUMBERS

1. Real numbers, absolute values and inequalities.
2. Sequences in $R$ and limits (finite and infinite) of such sequences.
3. Common criteria to study the convergence of a sequence in $R$ and to calculate its limit if it exists: Sandwich rule, monotonous sequences (the number e), Stolz criterion, equivalences (Stirling formula).
4. Series of real numbers. Geometric and harmonic series.
5. Convergence criteria: Gauss, quotient and Leibnitz.
6. Power series. Convergence radius.
7. Taylor Series. Bounding of the rest.

2 LIMITS AND CONTINUITY OF FUNCTIONS OF SERVERAL REAL VARIABLES.

1. Introduction to functions of several real variables with values in $R^{\wedge} n$.
2. Limit and continuity of functions of several real variables.
3. Directional and iterated limits. Limits in polar coordinates.

3 DERIVATION OF FUNCTIONS OF SERVERAL REAL VARIABLES.

1. Directional derivatives. Partial derivative. Gradient. Jacobian matrix.
2. Differentiable functions of several variables.
3. Properties of differentible functions. Chain rule. Change of variables
4. Partial derivatives of higher order. Hessian matrix.
5. Extremes of real functions of several real variables. Conditioned extremes. Lagrange multipliers.
6. Derivation of implicit functions.

## 7. ASSESSMENT METHODS AND CRITERIA

| Description | Type | Final Eval. | Reassessn | $\%$ |
| :--- | :--- | :--- | :--- | :--- |
| Quiz on the content of chapter 1 | Written exam | No | Yes | 30,00 |
| Quiz on the content of chapter 2 | Written exam | Written exam | No | Yes |
| Quiz on the content of chapter 3 | Written exam | No | Yes | 30,00 |
| Context problem. | No | No | 10,00 |  |
| TOTAL |  |  | 100,00 |  |
| Observations |  |  |  |  |

Continuous evaluation (ordinary call):
1st partial exam
2nd partial exam and recovery of first partial
3rd partial exam and recovery of second partial
Global problem.(Unrecoverable)

Extraordinary call: recovery of each of the partials.
Observations for part-time students
The same evaluation type applies to part time students

## 8. BIBLIOGRAPHY AND TEACHING MATERIALS

## BASIC

Material didáctico disponible en el Aula Virtual UC.
J.E. Marsden, A.J. Tromba. Cálculo Vectorial. Quinta edición. Pearson, Addison-Wesley, 2004.

