

School of Industrial Engineering and Telecommunications

# SUBJECT TEACHING GUIDE

## G424 - Calculus II

# Degree in Mechanical Engineering First Degree in Mechanical Engineering

### Academic year 2023-2024

1. IDENTIFYING DATA									
Degree	Degree in Mechanical Engineering First Degree in Mechanical Engineering			Type and Year	Core. Year 1 Core. Year 1				
Faculty	School of Industrial Engineering and Telecommunications								
Discipline	Subject Area: Mathematics Basic Training Module								
Course unit title and code	G424 - Calculus II								
Number of ECTS credits allocated	6	Term		Semeste	r based (2)				
Web	http://personales.unican.es/alvareze/CalculoWeb/CalculoII/index.html								
Language of instruction	Spanish	English Friendly	No	Mode of a	delivery	Face-to-face			

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Department	DPTO. MATEMATICA APLICADA Y CIENCIAS DE LA COMPUTACION		
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### **3.1 LEARNING OUTCOMES**

- -- Understand the concept of multiple integral using Riemann sums.
- Calculate curvilinear and surface integrals and know the physical interpretation of these concepts.
- Know and apply the main integral theorems of vector calculus.
- Obtain Laplace transform of functions and know their properties.
- Classify and solve some types of first order differential equations.
- Solve second order differential equations, linear homogeneous and non-homogeneous equations.
- Use mathematical software in problem solving as a tool of representation and calculation.



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#### 4. OBJECTIVES

Learn the main concepts of multiple integration and vector calculus. Apply these concepts to solve practical problems.

Learn the basic concepts of ordinary differential equations.

Know the theory and applications of the Laplace transform.

Use mathematical software to help solve problems.

### 6. COURSE ORGANIZATION

	CONTENTS						
1	Part 1. Multiple integration. Line integral. Surface integral						
1.1	<ul> <li>Topic 1. Multiple Integral</li> <li>1.1 Double integrals over a rectangle. Geometric interpretation. Existence and properties. Double integrals over regular domains. Change of variables in double integrals. Change of variables to polar coordinates. Applications.</li> <li>1.2 Triple Integrals over regular domains. Change of variables in triple integrals. Equations of common surfaces.</li> <li>Change of variables to cylindrical and spherical coordinates.</li> </ul>						
1.2	<ul> <li>Topic 2: Vector Fields and line integrals.</li> <li>2. Scalar and vector fields. Basic definitions. Differential operators. Conservative vector fields. Potential function.</li> <li>2.2 Line integrals. Differential element of arc length in cartesian, parametric and polar coordinates. Line integrals of a scalar field on a curve.</li> <li>2.3 Line integrals of a vector field on a curve.</li> <li>Green Theorem. Fundamental Theorem for line integrals. Theorem on conservative fields.</li> </ul>						
1.3	<ul> <li>Topic 3: Surface integrals.</li> <li>3.1 Definition of the differential element of surface in cartesian and parametric coordinates .</li> <li>3.2 Surface integrals of scalar fields. Properties. Applications.</li> <li>3.3 Surface integrals of vector fields or flux as a surface integral.</li> <li>Gauss Theorem or Divergence Theorem. Stokes Theorem.</li> </ul>						
2	Part II. Differential equations. LaplaceTransform.						
2.1	<ul> <li>Topic 4: Introduction to ordinary differential equations (ODE).</li> <li>4.1 Definition of differential equation. Order and degree. General solution and particular solutions of an ODE. Modelling by ODE: examples.</li> <li>4.2 Resolution of ordinary differential equations of first order: separable and reducible to separable equations; Exact equations and integrating factors; linear equations</li> <li>4.3 Resolution of linear ordinary differential equations of second order.</li> <li>4.4 Introduction to partial differential equations.</li> </ul>						
2.2	<ul> <li>Topic 5. Laplace Transform.</li> <li>5.1 Definition of Laplace transform of a function. Sufficient conditions of existence. Properties. Theorems.</li> <li>5.2 Inverse Laplace transform.</li> <li>5.3 Application of the Laplace transform to solve linear differential equations with constant coefficients and initial conditions.</li> </ul>						
2.3	Introduction to the Fourier Transform						



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7. ASSESSMENT METHODS AND CRITERIA								
Туре	Final Eval.	Reassessn	%					
Others	No	Yes	50,00					
Others	No	Yes	50,00					
Written exam	Yes	No	0,00					
TOTAL 100,00								
	Others Others	Others     No       Others     No	Others     No     Yes       Others     No     Yes					

#### Observations

In order to pass the subject in continuous or regular evaluation, it will be necessary that the notes of the 2 blocks are equal to or greater than 3 points out of 10. The weight of the parts are 50% for part I and 50% for part 2.

The students who have not passed the subject in ordinary call will have to sit the whole syllabus in extraordinary period. The mark obtained in the exam will represent the complete grade. When the grade obtained in the ordinary call in a block is higher than 4 points out of 10, this note may be kept for the extraordinary call.

In case of a lockdown imposed by the sanitary alert, the evaluation will be carried out using the telematics means offered by the University of Cantabria

Observations for part-time students

Part-time students can choose between the continuous assessment described above or opt to do the final exam. In the latter case, the exam mark obtained will represent the complete grade of the student for the subject.

#### 8. BIBLIOGRAPHY AND TEACHING MATERIALS

BASIC

Material proporcionado por el profesorado:

- Página web de la asignatura: http://personales.unican.es/alvareze/CalculoWeb/CalculoII/index.html
- Pagina web con ejercicios interactivos Giematic UC: http://www.giematic.unican.es
- Página de la asignatura en Moodle

Cálculo Vectorial. Parte II. Juan Guillermo Rivera. Elena Álvarez

https://proyectodescartes.org/iCartesiLibri/materiales\_didacticos/Calculo\_III\_parte2/index.html

Larson, R. y Edwards, B. H. Cálculo 2 de varias variables. Editorial Mc Graw-Hill.

Disponible en la biblioteca: http://catalogo.unican.es

Nagle, R. K. y Staff, E. B. "Ecuaciones diferenciales con valores en la frontera". Editorial Addison-Wesley.

Disponible en la biblioteca: http://catalogo.unican.es